Catch and Release of Microwave Photon States

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We demonstrate a superconducting resonator with variable coupling to a measurement transmission line. The resonator coupling can be adjusted through zero to a photon emission rate 1000 times the intrinsic resonator decay rate. We demonstrate the catch and release of photons in the resonator, as well as control of nonclassical Fock states. We also demonstrate the dynamical control of the release waveform of photons from the resonator, a key functionality that will enable high-fidelity quantum state transfer between distant resonators or qubits.

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Superconducting resonators play a central role in quantum information technology. Applications include the synthetic generation and storage of photon quantum states [1-3], quantum memories for quantum computation [4], and dispersive measurements of superconducting qubits [5,6], as well as defects in diamond [7,8]. Resonators with low internal losses are typically desirable, but the resonator's coupling strength to the quantum system and to its measurement apparatus is application dependent. When coupling a resonator to a qubit, either for a quantum memory or in a circuit quantum electrodynamics [5] experiment, strong coupling to the qubit improves information transfer but also increases dephasing. When reading out a qubit, coupling the resonator strongly to its measurement apparatus increases the measurement bandwidth and signal but in addition increases dissipation [9]. Resonator designs therefore involve compromises between the competing needs for both strong and weak coupling [10,11]. A resonator with a variable coupling would provide a significant improvement: If used to measure a qubit, the coupling to the measurement apparatus could be turned off except during resonator readout, when the coupling could be made large. When coupling two qubits through a resonator, the coupling could be turned on and off as needed [12,13], yielding higher fidelity gates [14,15].

Here we employ an externally controlled variable inductance [16] to modulate the coupling of a resonator to a transmission line, creating the microwave equivalent of a Fabry-Perot cavity with a variable-transparency mirror. The resonator also has fixed coupling to a superconducting phase qubit. We demonstrate the time-controlled release of single-photon Fock and superposition states, thus generating a "flying qubit" [17-19]. We also perform timed capture and release of few-photon coherent states, and use the variable coupling to transmit and release photons with arbitrary waveforms [20,21]. This new capability promises numerous applications in high-fidelity quantum computing and communication.

The schematic in Fig. 1(a) displays a Fabry-Perot cavity, which represents the resonator, with a tunable transparency mirror to represent the variable coupler. A two-level atom plays the role of the qubit. In the actual experiment [Figs. 1(b) and 1(c)], the resonator (r) is a quarterwavelength $(\lambda/4)$ coplanar waveguide resonator, with one end coupled to a superconducting phase qubit (q)and the other end shorted to ground. Close to the grounded end (a distance $\sim \lambda/60$ away), the resonator is connected to a variable coupler (c), a transformer comprising two fixed inductors L_1, L_2 , and a superconducting quantum interference device (SQUID) with tunable inductance L_s . A bias

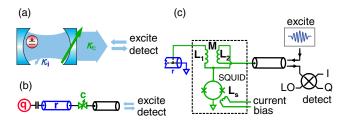


FIG. 1 (color online). Experimental setup. (a) Schematic for a cavity with a variable transparency mirror, where κ_c is the decay rate through the variable mirror and κ_i the intrinsic photon decay rate. (b) Experimental schematic. The resonator r is capacitively coupled to a superconducting phase qubit q at the left end, and connected to a transmission line through a variable coupler c at the right end. (c) Details of the variable coupler and the electronic control. Microwave excitation signals drive the resonator through the transmission line, and signals from the resonator are amplified and demodulated using a mixer driven by a local oscillator (LO). The demodulated I and Q signals oscillate at the LO sideband frequency.

current controls the variable coupler and modulates the coupling to a microwave transmission line by flux tuning the SQUID inductance embedded in the mutual inductance circuit. We want to emphasize that, although a junctiontype variable coupler has been used to couple two qubits [16], here the coupling to the transmission line in place of a qubit requires a complete redesign of the coupling element, as detailed in the Supplemental Material [22].

The resonator-transmission line coupling κ_c can vary from zero to a maximum emission rate $\kappa_{\text{max}} \approx 1/(5 \text{ ns})$, over a time scale of a few nanoseconds. The resonator frequency is $f_r \approx 6.57$ GHz, and the phase qubit has a ground to excited state ($|g\rangle \leftrightarrow |e\rangle$) transition frequency tunable from ~6 to 7 GHz [2,16,23]. The qubit-resonator coupling, $g/2\pi \approx 12$ MHz, is calibrated by swap spectroscopy [4], in which the population of qubit excitation is measured as a function of qubit-resonator detuning and interaction time. The qubit-resonator interaction is controlled by tuning the qubit frequency, and is effectively turned off by setting the qubit frequency to its idle point, 400 MHz below the resonator frequency [2,16,23].

The resonator and variable coupler were characterized by measuring the decay of a one-photon Fock state stored in the resonator. When the resonator is weakly coupled to the transmission line, the photon decays due to internal resonator losses, while when strongly coupled, the photon is emitted into the transmission line. The pulse sequence is shown in Fig. 2(a) (top), where the qubit was excited from $|g\rangle$ to $|e\rangle$, and the excitation then swapped to the resonator by an ISWAP pulse, creating a one-photon Fock state [2]. The coupler bias current was then adjusted [Fig. 2(a), middle] from zero to a variable amplitude which set the coupling strength. After a delay time τ , the residual excitation was swapped back to the qubit, and the qubit measured.

Figure 2(b) displays the probability P_e of measuring the qubit in $|e\rangle$ as a function of delay τ and the variable coupler current bias. P_e decays exponentially with time τ , with the decay rate varying strongly with coupler bias. Two line cuts are shown in Fig. 2(d), with exponential fits yielding the resonator lifetime T_1 . For zero coupling, as determined by maximizing T_1 with respect to coupler bias, we find the intrinsic $T_{1,i} \approx 4.5 \ \mu$ s, in agreement with resonator loss measurements, while for coupling κ_{large} the lifetime $1/T_1$ is the sum of the intrinsic decay rate $1/T_{1,i}$ and the coupler emission rate κ_c , so $\kappa_c = 1/T_1 - 1/T_{1,i}$. The coupling dependence on current bias in Fig. 2(b) is in good agreement with calculations, as shown in Fig. 2(c) (see details in the Supplemental Material [22]).

We demonstrated dynamic control by changing the coupling during the delay period, as shown in Fig. 2(e). We started with the coupling set to zero, and after a delay τ_s switched the coupling to $\kappa_{\text{large}} \simeq 1/(30 \text{ ns})$ [Fig. 2(a), bottom]. The reduction in the photon lifetime after the switch

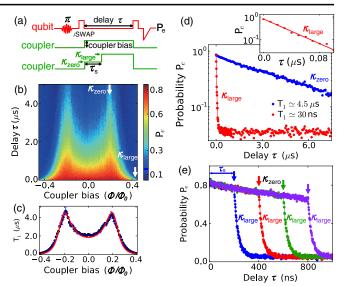


FIG. 2 (color online). Characterization of the variable coupler with Fock state $|1\rangle$. (a) Pulse sequence for the qubit (top) and coupler [middle used in (b) and (c); bottom used in (d)], with details described in the text. The qubit measurement is a projective single-shot procedure, with 600 averages yielding the qubit excited state probability P_e . (b) P_e (color scale) versus τ (vertical axis) and coupler bias in flux units (horizontal axis). (c) The resonator lifetime T_1 extracted from data in (b) is displayed as blue dots, compared with the theoretical evaluation of T_1 (shown as a red line, and see details in the Supplemental Material [22]). (d) Vertical line cuts of (b) display exponential decay of P_e , which gives resonator lifetime T_1 . Inset shows P_e for short times for κ_{large} . (e) P_e versus delay τ for coupling strength switching from zero to κ_{large} . Decay rate switches from intrinsic lifetime (4.5 μ s) to 30 ns, with transition taking \sim 2 ns. Blue, red, green, and purple lines correspond to switching delays τ_s of 200, 400, 600, and 800 ns, respectively.

is clearly visible. The upper bound of κ_{zero} is smaller than 0.1 MHz in our system [16]. The coupler switching speed was limited by the ~2 ns rise time of the coupler bias, roughly 2000 times shorter than $T_{1,i}$.

This measurement does not distinguish between incoherent decay and the expected phase-coherent release of the photon. We therefore also used heterodyne detection, with the resonator "catching" and then "releasing" photons in coherent states. Figure 3(a) displays the pulse sequence: With the coupler set to an intermediate coupling $\kappa_c = 1/(356 \text{ ns})$, we excited the resonator with a 100 ns Gaussian pulse from the microwave source, with the pulse calibrated to trap $\langle n \rangle = 10$ photons (see Supplemental Material [22]). The coupling was then set to zero, trapping the photons for a storage time τ_s , then set back to $\kappa_c = 1/(356 \text{ ns})$, releasing the photons for heterodyne detection.

Figure 3(b) shows the heterodyne-detected signal in the I (real) and Q (imaginary) quadratures in the time domain. During the Gaussian excitation pulse, the signal comprised the reflected component of the excitation. No signal was detected during the subsequent $\tau_s = 200$ ns storage time

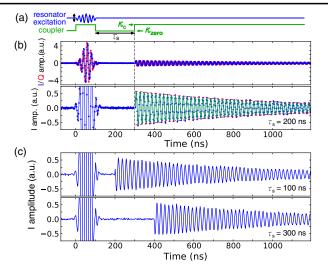


FIG. 3 (color online). Catch and release of photons in coherent states. All traces averaged 10^5 times. (a) Pulse sequence. Resonator (blue) is driven by on-resonance, 100 ns Gaussian excitation pulse, and coupler (green) tuned to $\kappa_c \simeq 1/(356 \text{ ns})$. Photons are stored for time τ_s at zero coupling, then released with $\kappa_c = 1/(356 \text{ ns})$. (b) Top panel: Demodulated I and Q quadrature signals for $\tau_s = 200$ ns, with 50 MHz sideband oscillations and a relative $\pi/2$ phase shift (lines are guides to the eye). Signals include reflected part of excitation pulse, followed by release signal after delay τ_s , comprising a sudden onset with exponential decay. Results are given in arbitrary units (a.u.). Bottom panel: I on expanded scale, with sinusoidal fit (thick green line), comprising sideband oscillations with exponential decay envelope (dashed red line, time constant $T_d =$ 706 ns). The fixed phase with 10^5 averages indicates phase coherence of photon release. (c) I quadrature for trapping delays $\tau_s = 100$ and 300 ns, showing excitation pulse and a delayed photon release.

with the coupler turned off. A sharp onset followed by an exponentially decaying envelope appeared when the coupler was turned back on, releasing the photons. The signal envelope has a decay time $T_d = 706$ ns, in close agreement with the expected value $2/\kappa_c = 712$ ns. The amplitude oscillations are from a 50 MHz mixer sideband signal, and the *I* and *Q* quadratures have a relative $\pi/2$ offset, as expected. As the output traces were averaged 10⁵ times, the presence of oscillations indicates that the output represents coherent photon release, with a fixed output phase relative to the input. The catch efficiency in this procedure is 13% (its theoretical estimation is 19%) and will be optimized in the future [24].

Figure 3(c) displays the *I* quadratures using storage times $\tau_s = 100$ and 300 ns. These are identical during the state-generating Gaussian pulse, but during the release the oscillation phase depends on the storage time τ_s , scaling as $\sim 0.81 \pi (\tau_s/100 \text{ ns})$. This phase accumulation is as expected from the small tuning of the resonator frequency f_r with coupler bias (see Supplemental Material [22]), further demonstrating the coherence of the release. We also calculated the radiated energy $\int_{t_r}^{t_c} [I^2(t) + Q^2(t)]dt$, integrating the signal power from the photon release time t_r to a cutoff $t_c = t_r + 3T_d$. We find that the released energy for $\tau_s = 300$ ns is 4% lower than for $\tau_s = 100$ ns, in agreement with the expected intrinsic resonator loss.

These measurements confirm the phase-coherent capture and release of coherent states. To demonstrate that we can achieve the same control for nonclassical states, we used the qubit to generate [2] the photon superposition state $(|0\rangle + |1\rangle)/\sqrt{2}$ and measured the release signal after turning on the coupling [Fig. 4(a)]. For an intermediate coupling $\kappa_c \simeq 1/(320 \text{ ns})$ and a large coupling $\kappa_c \simeq 1/(30 \text{ ns})$, the signal's exponential decay envelope has a time constant $T_d \approx 625$ and 69 ns, respectively, close to the expected $2/\kappa_c$, verifying that the coupling determines

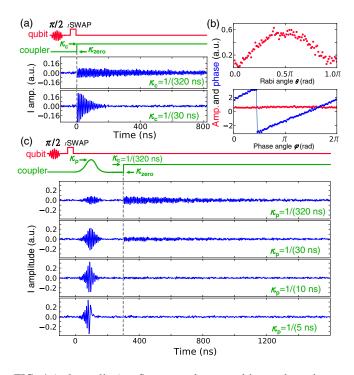


FIG. 4 (color online). Storage, release, and heterodyne detection of nonclassical photon states. (a) Top: Pulse sequence to prepare a superposition Fock state $(|0\rangle + |1\rangle)/\sqrt{2}$ and release this nonclassical photon state. Coupler is switched at t = 0 from zero to a coupling κ_c . Middle and bottom: Heterodyne-detected I quadrature for two κ_c values. Mixer LO sideband frequency is 110 MHz, with 10^6 averages. (b) Amplitude (red) and phase (blue) of demodulated signal for the released superposition state $\cos(\theta/2)|0\rangle + e^{i\phi}\sin(\theta/2)|1\rangle$. The measurement is taken with 3.6×10^5 averages. (c) First panel: Tailored, two-segment release pulse sequence for $(|0\rangle + |1\rangle)/\sqrt{2}$ superposition state, using a 200 ns Gaussian control pulse followed by a rectangular pulse, with intervening 100 ns delay. Second to fifth panels: Pulse amplitude κ_p set to different values as shown. I quadrature amplitude depends on κ_p , with different amounts of energy released during Gaussian pulse; two top panels show remainder released during final rectangular pulse.

the release rate. The integrated energy for intermediate coupling is 7% lower than for large coupling, attributed to greater intrinsic loss from the slower release.

We next tested the release and detection of the qubitprepared superposition state $\cos(\theta/2)|0\rangle + e^{i\phi}\sin(\theta/2)|1\rangle$, akin to previous work with static coupling [17,18]. After state preparation, the variable coupling was changed from zero to $\kappa_c = 1/(320 \text{ ns})$, and the released photons were heterodyne detected as a function of the Rabi angle θ and the phase angle ϕ , with Fourier transforms of I and Q yielding the signal amplitude and phase. Figure 4(b) shows the dependence of the signal amplitude on θ , with $\phi = 0$. The maximum amplitude is at $\theta = \pi/2$, corresponding to $(|0\rangle + |1\rangle)/\sqrt{2}$. The amplitude goes to zero for the pure Fock states at $\theta = 0$ and π as expected, due to the loss of phase coherence at the Bloch sphere poles. When releasing the state $(|0\rangle + e^{i\phi}|1\rangle)/\sqrt{2}$ with $\theta = \pi/2$ and varying ϕ , the signal has constant amplitude (0.613 ± 0.066) and phase increasing linearly with ϕ .

The on-demand, real-time gating of the coupler enables precise shaping of the photon release waveform. Figure 4(c)shows the tailored time-dependent release of the $(|0\rangle +$ $|1\rangle)/\sqrt{2}$ photon state, modulating the coupling with a 200 ns Gaussian bias pulse with peak coupling κ_p , followed by a 100 ns delay and then completing the release with $\kappa_c = 1/(320 \text{ ns})$. Figure 4(c) shows the *I* quadrature signal for $\kappa_p = 1/(320 \text{ ns}), 1/(30 \text{ ns}), 1/(10 \text{ ns}), and$ 1/(5 ns), with a Gaussian-like release waveform mimicking the coupler pulse. For the top three panels, energy integrals show that 17.5, 43.1, and 100% of the total stored energy is released during the pulse, with the remainder released after the 100 ns delay. For couplings $\kappa_n \gtrsim$ 1/(10 ns), the release is completed during the Gaussian pulse. In contrast to fixed coupling, in which the waveform decays exponentially with time, this experiment shows carefully shaped waveforms, a critical feature needed for high-fidelity transfer of photonic information [14,15].

In conclusion, we have realized a superconducting resonator with a completely controllable mirror transparency. While an adjustable cavity-environment coupling has been speculated using interference effect [25,26] or manipulation of energy levels [27], this is the first experimental demonstration of a variable transparency mirror in any system. We have demonstrated the phase-coherent, controlled capture and release of coherent and superposition photon states from a resonator, using a resonatortransmission line variable coupling. The catch and release of photons has attracted significant attention in atomic and planar photonic systems [20,26,27]. Our work extends prior coherent state demonstrations to the microwave domain, along with release of nonclassical photon states with a more complete characterization. This powerful technique should allow long-range entanglement [4,28–32], where the shaped release we display in the last experiment is a key ingredient for high-fidelity state transfer [14,15]. This capability will further enable tunable coupling for resonator-based dispersive qubit readout, where timedomain control can minimize deleterious dephasing while maximizing measurement bandwidth and signal strength.

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